



Photronics Center, Laboratory for Photoacoustics,
Institute of Physics, Belgrade, Serbia

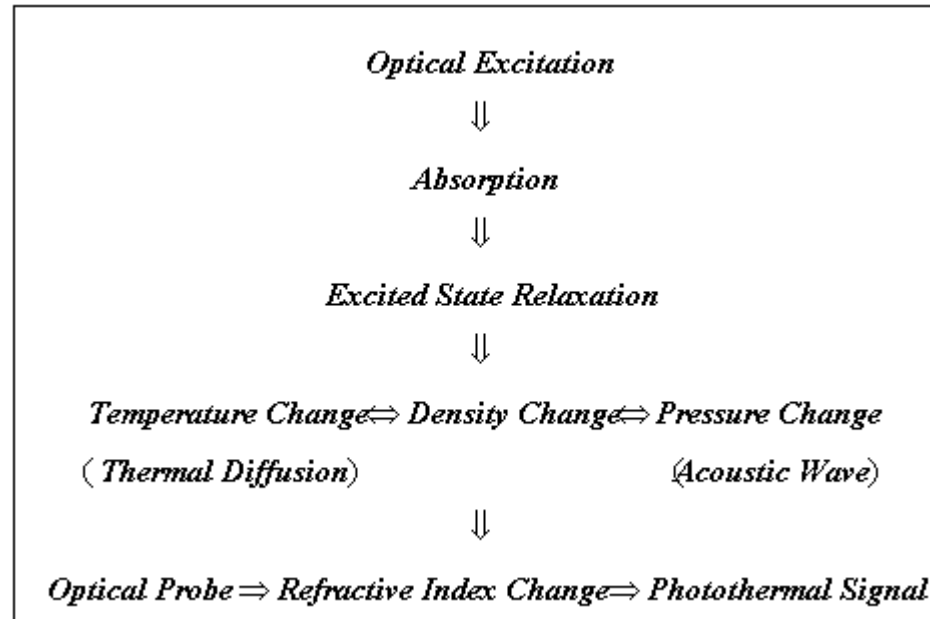


L3 – Photothermal techniques in material characterization

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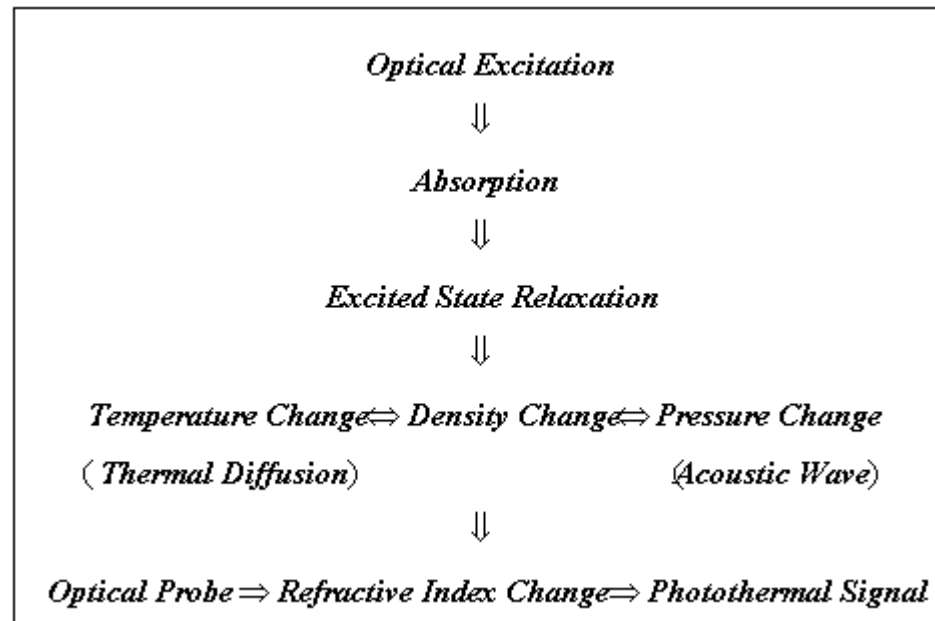


Photothermal spectroscopy is a group of high sensitivity methods used to measure optical absorption and thermal characteristics of a sample.



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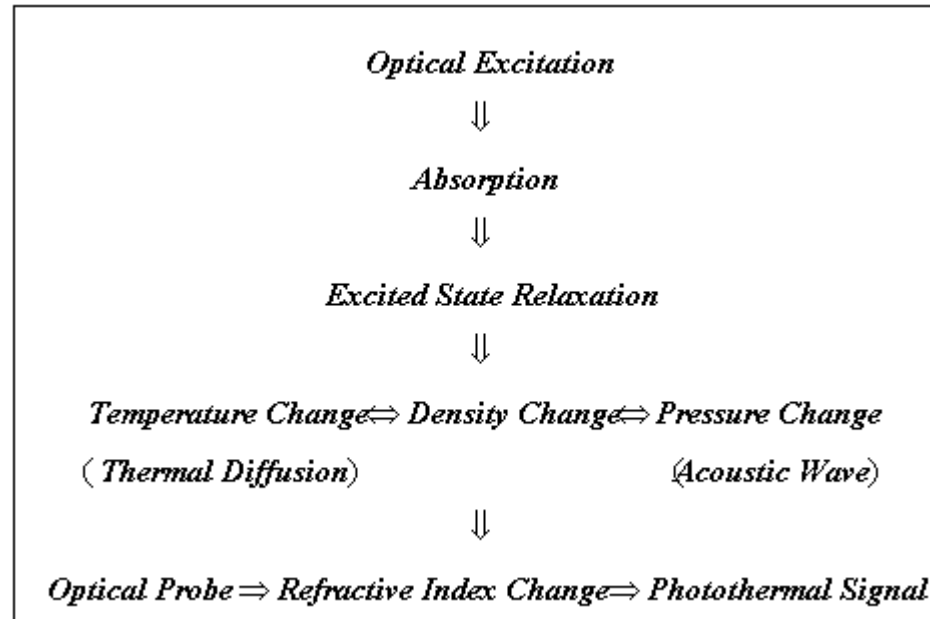


The basis of photothermal spectroscopy is a *photo*-induced change in the *thermal* state of the sample.



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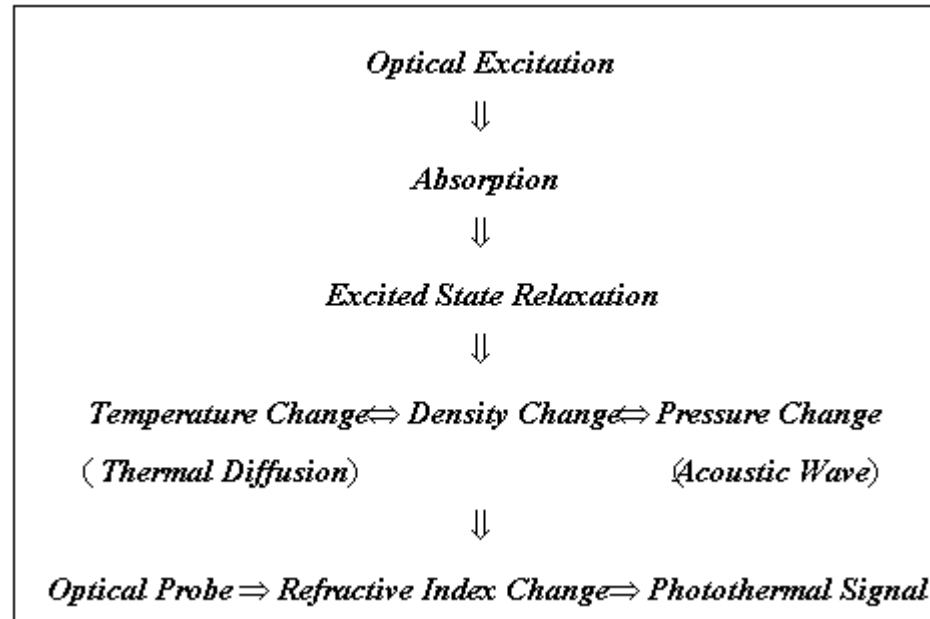


Light energy absorbed and not lost by subsequent emission results in sample heating.



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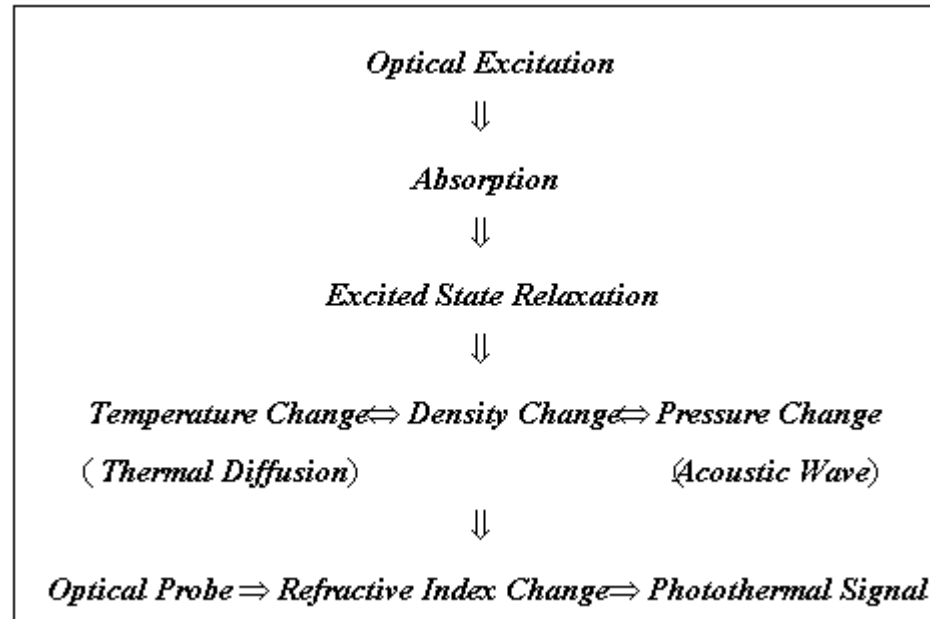


This heating results in a temperature change as well as changes in thermodynamic parameters of the sample which are related to temperature.



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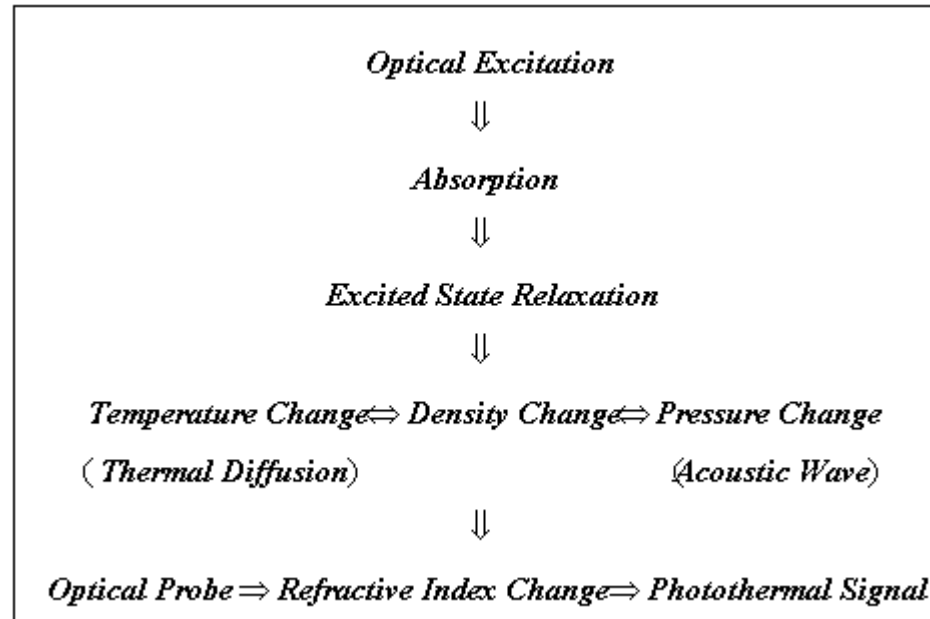


Indirect measurement of the temperature, pressure, or density changes that occur due to optical absorption are ultimately the basis for the photothermal spectroscopic methods.



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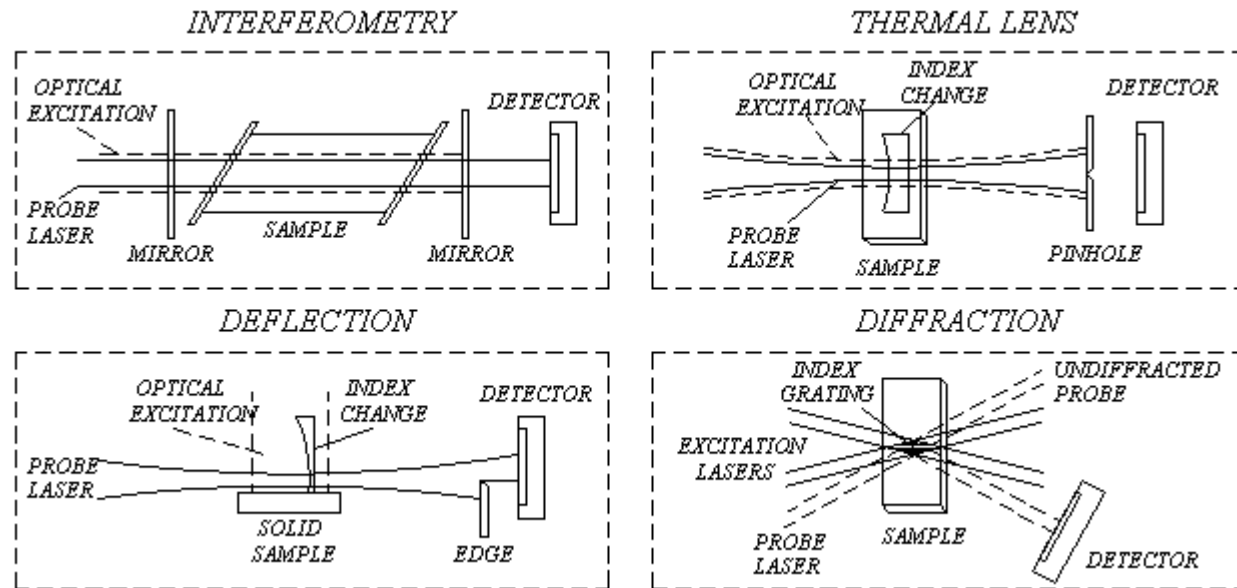


Most of Photothermal spectroscopic methods are nondestructive, accurate, precise and reliable operating usually in real time.



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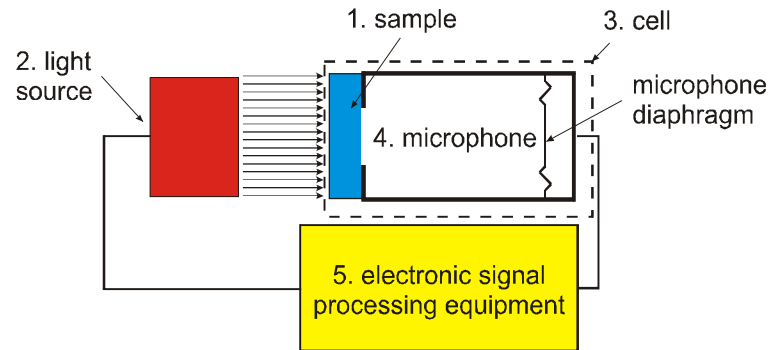


Interferometry directly measures the refractive index. Deflection measures the gradient. Thermal lens spectroscopy is based on beam focusing or defocusing. Diffraction methods measure the power of a beam diffracted by the periodic index.



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In photoacoustics modulation of the light impinging on an absorbing substance will produce a similar modulation in temperature through the photothermal effect. In a gas of restricted volume, temperature modulation produces a pressure modulation. The periodic pressure modulation is an acoustic signal.



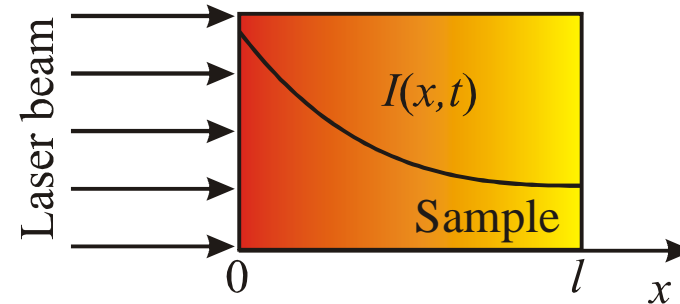
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Temperature Distributions in Semiconductors

Sample Heating



$$j_Q(x,t) = -k \frac{\partial T}{\partial x}$$



$$\frac{\partial j_Q}{\partial x} + \rho c \frac{\partial T}{\partial t} = 0$$



$$\frac{\partial T}{\partial t} = D_T \frac{\partial^2 T}{\partial x^2}$$



$$D_T = \frac{k}{\rho c}$$

$$I = I_0 \operatorname{Re}(1 + e^{i\omega t})$$



Modulated

$$T(x,t) = T_{dc}(x) + \operatorname{Re}(T(x)e^{i\omega t})$$

Steady state

$$\frac{\partial^2 T_{dc}}{\partial x^2} = 0$$

$$\frac{\partial^2 T}{\partial x^2} - \frac{i\omega}{D_T} T = 0$$



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Temperature Distributions in Semiconductors

$$\frac{d^2 T_s(x)}{dx^2} - \sigma^2 T_s(x) = -\frac{1}{k} \left[\frac{\varepsilon - \varepsilon_g}{\varepsilon} \beta I_0 \exp(-\beta x) - \frac{\varepsilon_g}{\tau} \delta n_p(x) \right]$$

$$\text{a) } -k \left. \frac{\partial T(x)}{\partial x} \right|_{x=0} = s_1 \delta n_p(0) \varepsilon_g$$

$$\text{b) } -k \left. \frac{\partial T(x)}{\partial x} \right|_{x=l} = -s_2 \delta n_p(l) \varepsilon_g$$

$$T_{\text{therm}}(x) = \frac{I_0}{k} \frac{\varepsilon - \varepsilon_g}{\varepsilon} \frac{\beta}{\beta^2 - \sigma_i^2} \left[b \frac{e^{\sigma_i(x-l)} + e^{-\sigma_i(x-l)} - e^{-\beta l} (e^{\sigma_i x} + e^{-\sigma_i x})}{e^{\sigma_i l} - e^{-\sigma_i l}} - e^{-\beta x} \right]$$

$$T_{\text{br}}(x) = \frac{\varepsilon_g B_1}{\tau k \sigma_i^2} \left\{ \frac{B_2 e^{\sigma_i x} + B_3 e^{-\sigma_i x}}{e^{\sigma_i l} - e^{-\sigma_i l}} - \frac{1}{c^2 - 1} \left[\frac{\delta n_p(x)}{B_1} + \frac{b^2 - c^2}{b^2 - 1} e^{-\beta x} \right] \right\}$$

$$T_{\text{sr}}(x) = \frac{2\varepsilon_g}{k\sigma} \frac{s_1 \delta n_p(0) \cosh[\sigma(x-l)] + s_2 \delta n_p(l) \cosh(\sigma x)}{e^{\sigma l} - e^{-\sigma l}}$$

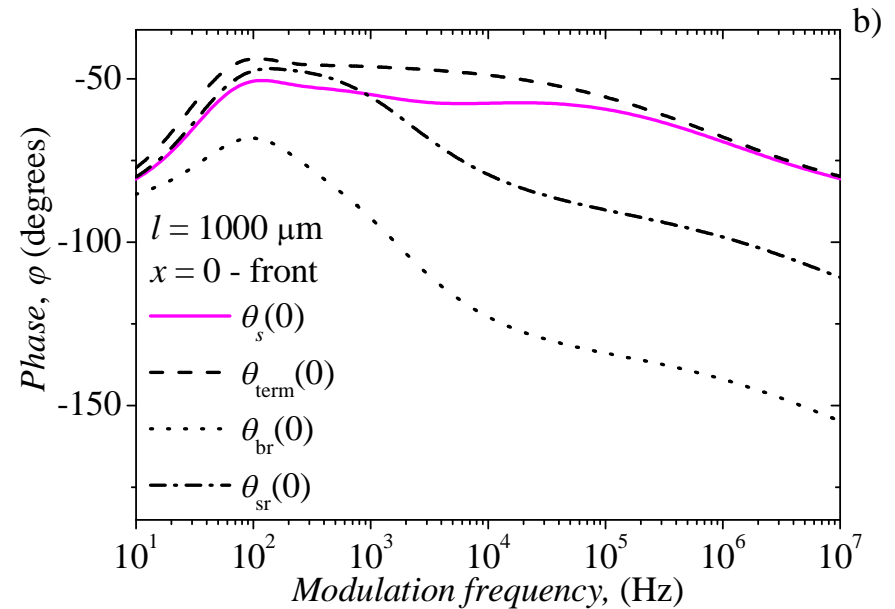
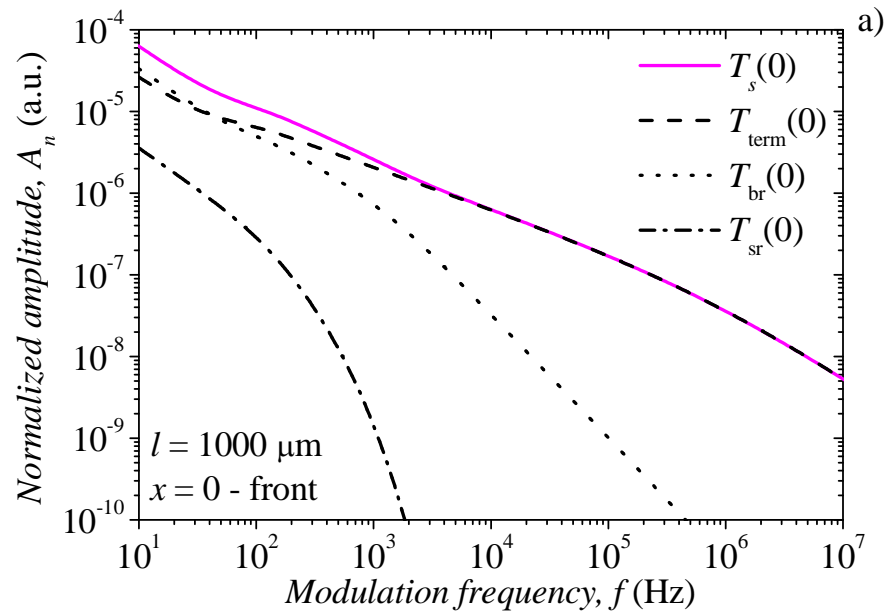
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Temperature Distributions in Semiconductors – at front (0) and back (l)

$$T_s(0) = T_{\text{therm}}(0) + T_{\text{br}}(0) + T_{\text{sr}}(0)$$



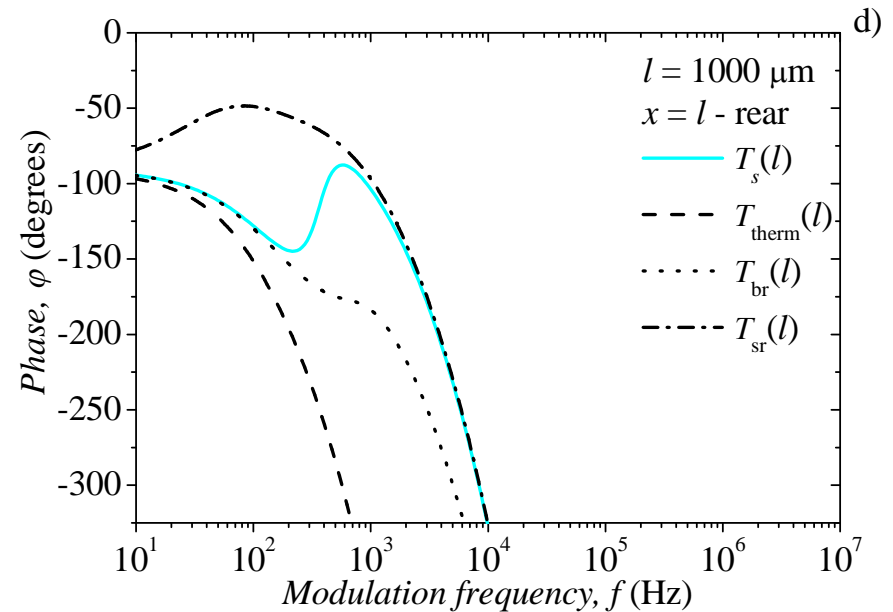
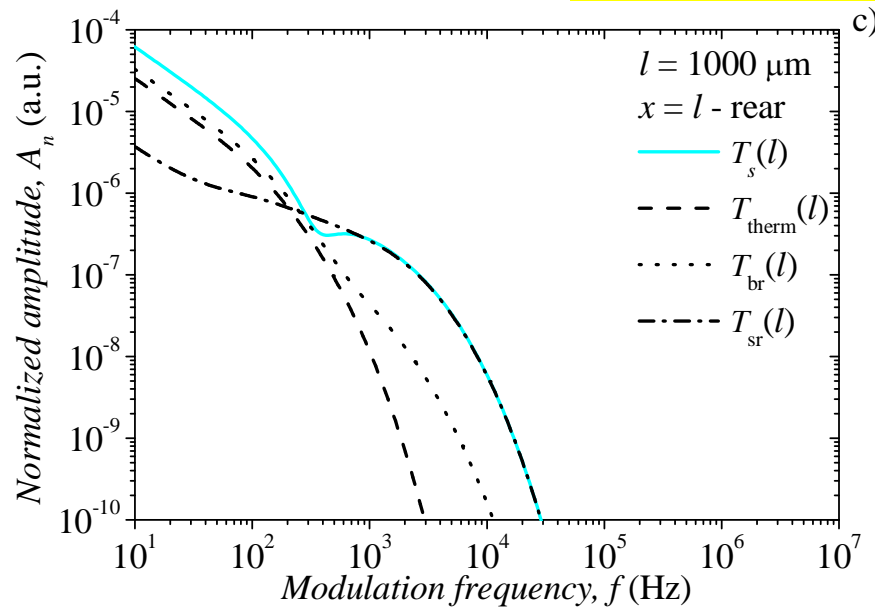
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Temperature Distributions in Semiconductors – at front (0) and back (l)

$$T_s(l) = T_{\text{therm}}(l) + T_{\text{br}}(l) + T_{\text{sr}}(l)$$



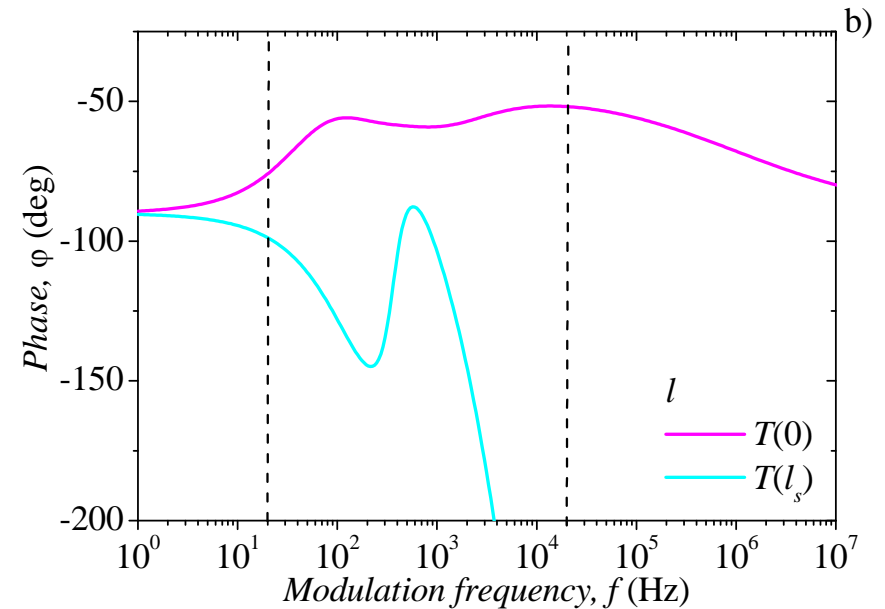
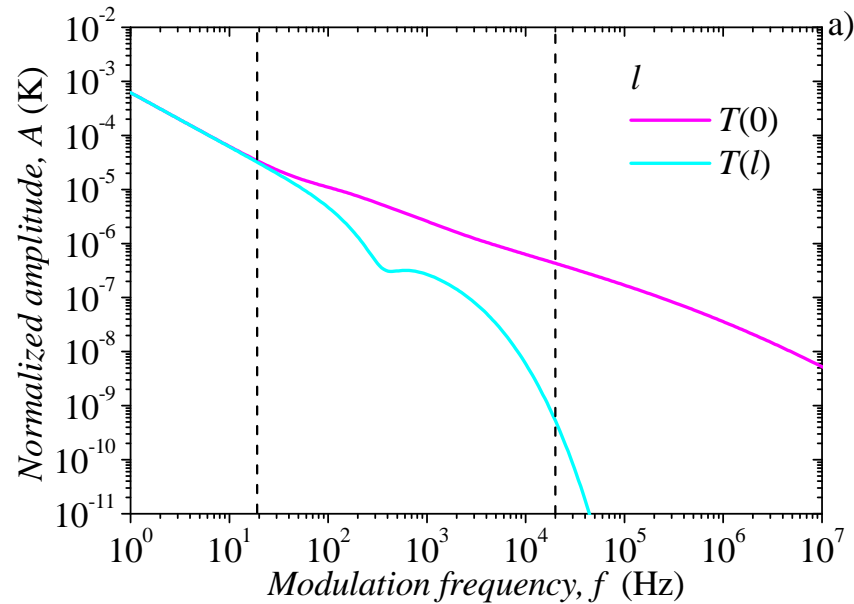
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Temperature Distributions in Semiconductors – at front (0) and back (l)

$$T_s(x) = T_{\text{therm}}(x) + T_{\text{br}}(x) + T_{\text{sr}}(x)$$

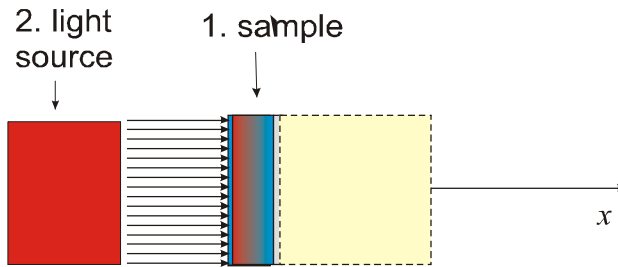


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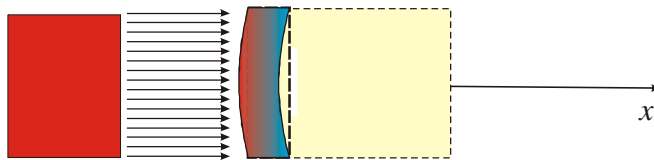




Photoacoustic Signal Generation in Semiconductors



$$\delta p_{\text{TD}}(f) = \frac{\gamma_g p_0 \sqrt{D_g}}{l_c T_0 \sqrt{2\pi f}} T_s(l)$$



$$\delta p_{\text{TE}}(f) = 3\pi \cdot \alpha \frac{\gamma_g p_0}{V_0} \frac{R_s^4}{l^3} \int_0^l \left(x - \frac{l}{2}\right) \cdot T_s(x) dx$$

$$\delta p_{\text{PE}}(f) = 3\pi \cdot d_n \frac{\gamma_g p_0}{V_0} \frac{R_s^4}{l^3} \int_0^l \left(x - \frac{l}{2}\right) \cdot n(x) dx$$

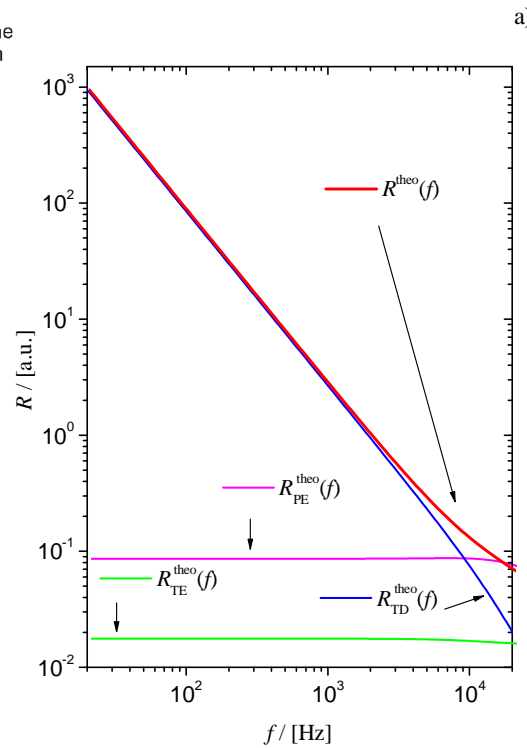
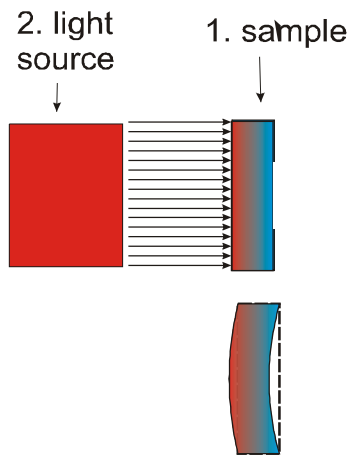
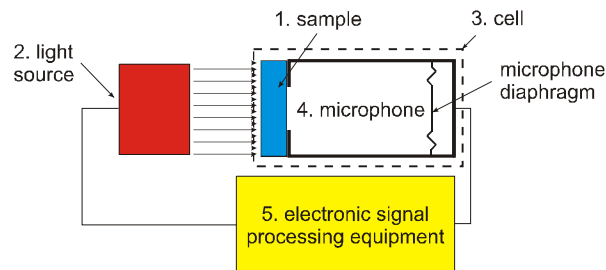
$$\delta p(f) = \delta p_{\text{TD}}(f) + \delta p_{\text{TE}}(f) + \delta p_{\text{PE}}(f)$$

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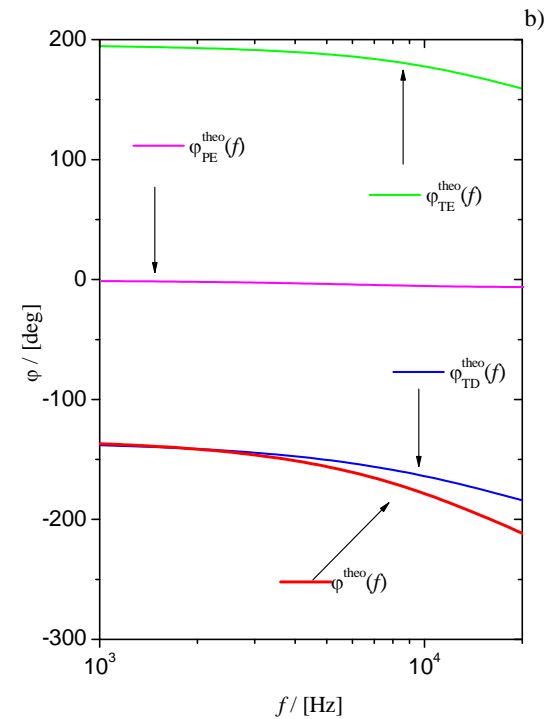




Photoacoustic Signal Generation in Semiconductors



Si sample, thin plate

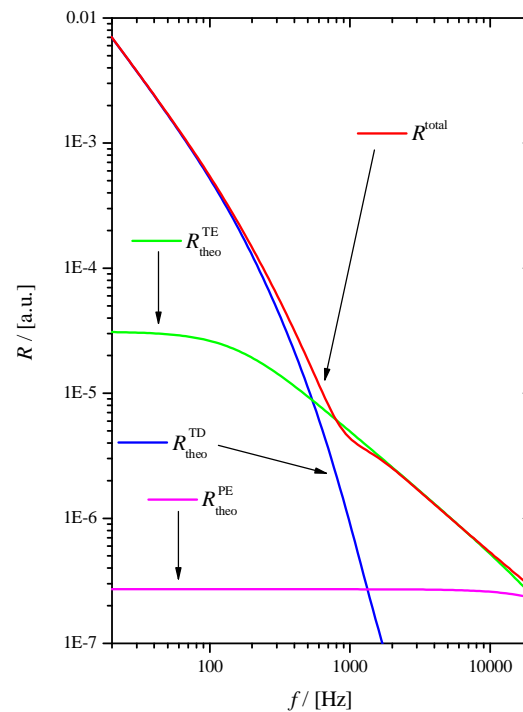
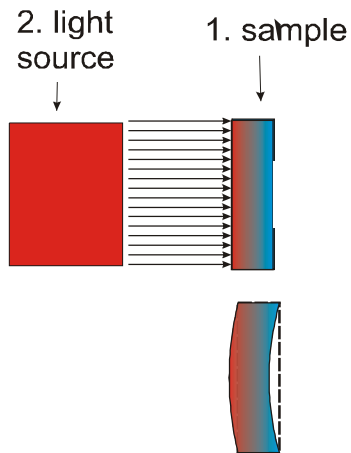
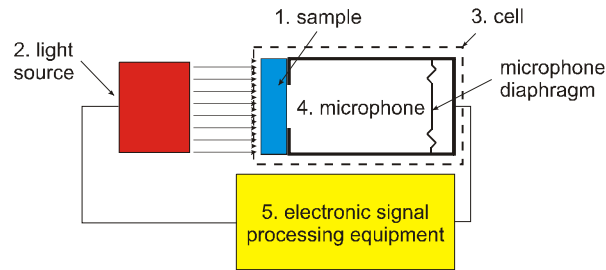


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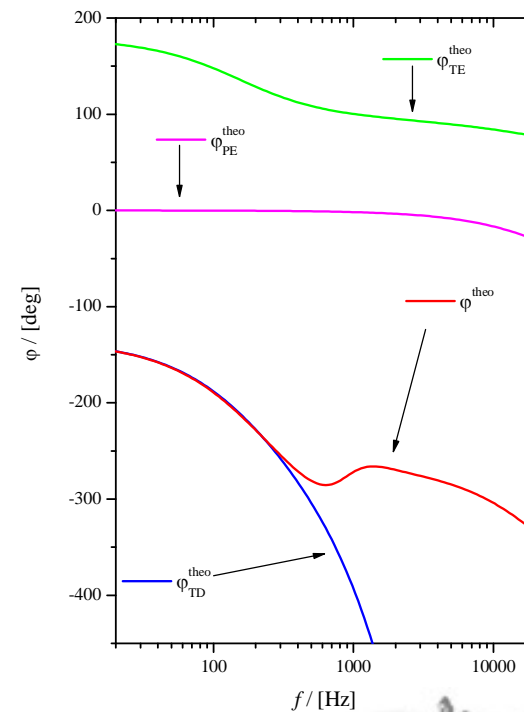




Photoacoustic Signal Generation in Semiconductors



Si sample, thick plate

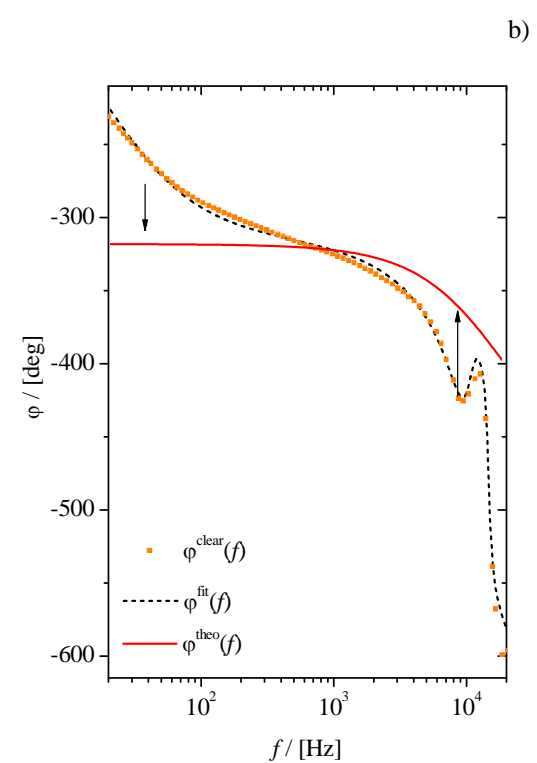
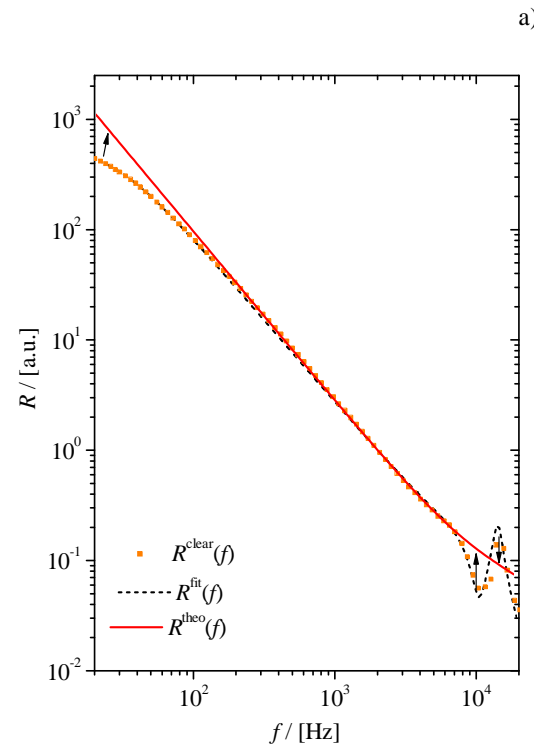
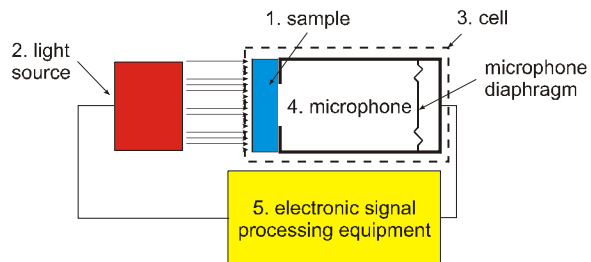


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Open photoacoustic cell technique: Measurement procedure

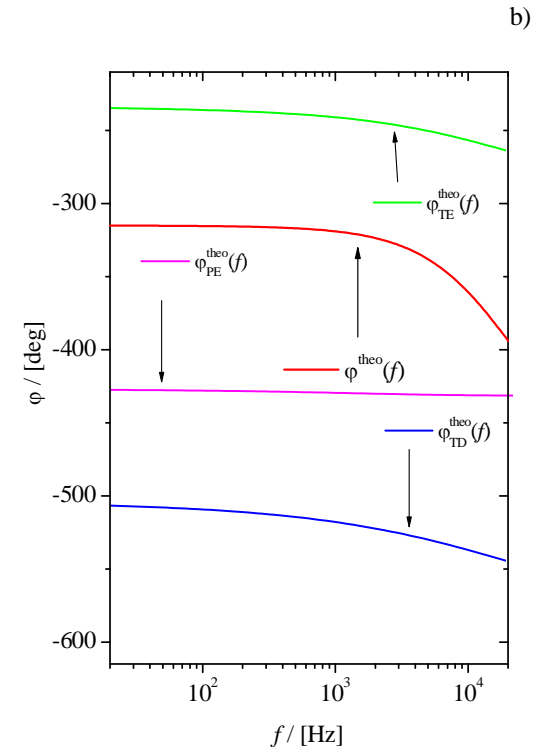
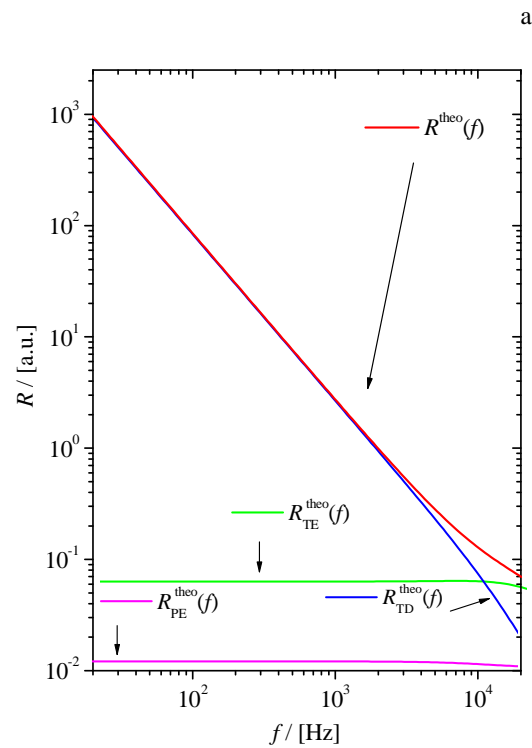
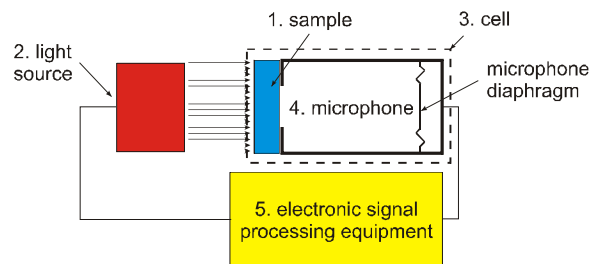


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Open photoacoustic cell technique: Measurement procedure – macro and microstructures



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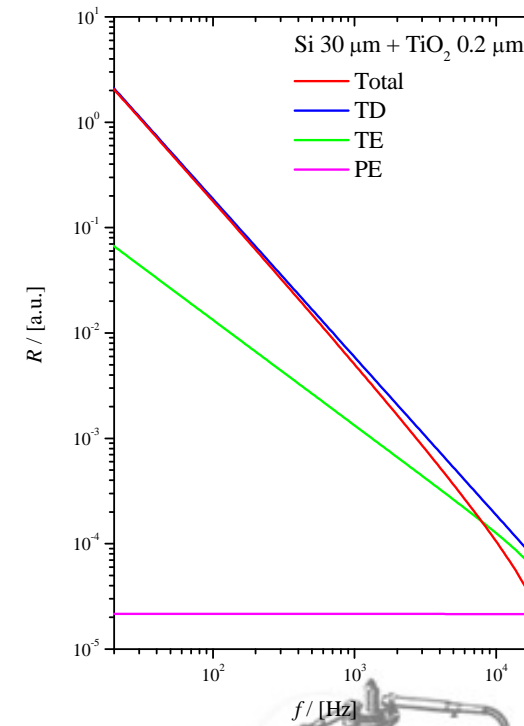
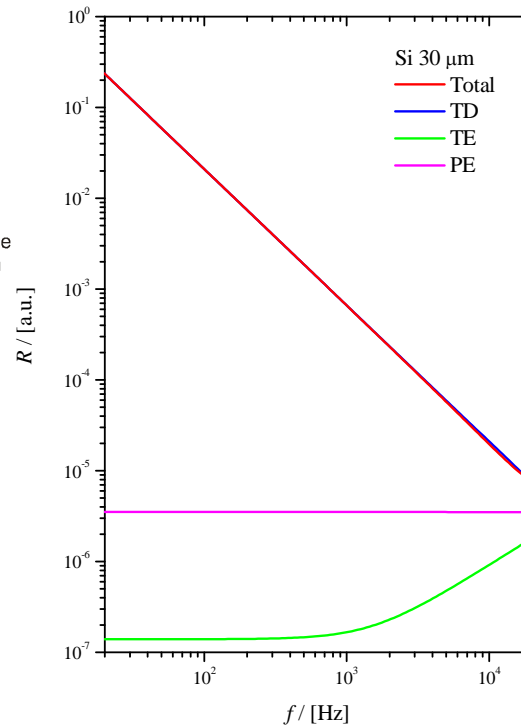
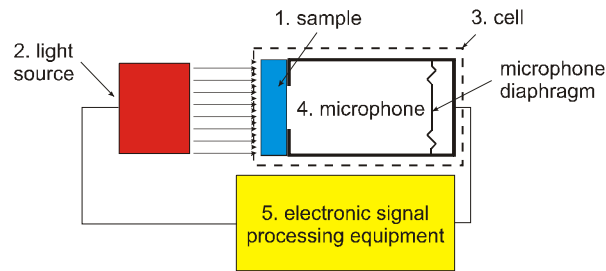




Open photoacoustic cell technique: Measurement procedure – micro- and nano-structures

Si 30 μm one-layer system

Si + TiO₂ two-layer system



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